A New Method Based On Evidence Theory and Fuzzy Clustering For the Breast Cancer Cells Images Segmentation

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Abstract: In this paper, a new method is proposed to segment the cells images especially when only one breast cancer cells image is available for each patient. The method is approached by fusing the information of pixels coming from the original image and different information pixels associated to the same original image represented in another space colors with Dempster–Shafer (DS) theory. The estimation of the mass functions of each single hypothesis is obtained from the membership function of applying fuzzy c-means (FCM) clustering to the gray levels coming from the images to be combined. Then, multiple hypotheses are generated according to the single hypothesis. The classification accuracy of the proposed method is evaluated and a comparative study versus existing techniques is presented. The experimental results on medical and synthetic color images demonstrate the value of introducing fuzzy clustering in the data fusion theory for image segmentation.

Key words: Breast cancer cells images, color, segmentation, fuzzy c-means, Dempster–Shafer's evidence theory, fuzzy clustering, conflict.

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1. Introduction

Image segmentation [1] [2], is one of the key tasks in most image processing and computer vision applications. The purpose of image segmentation is to divide images into different regions for future processing based on given criteria [3] [4] [5] [6]. At present, color image segmentation methods [7] [8], are mainly extended from gray level segmentation approaches by being implemented in different color space. Gray level segmentation methods are directly applied to each component images of color space, then the combination rule and decision related to a particular fusion theory are used to achieve the final segmentation result [9] [10] [11] [12].

In this context, Max Mignotte [8] has proposed the fusion model which combines the several input segmentations in the within-cluster variance sense since in order to get the final accurate segmentation result by employing a K-means algorithm based fusion scheme. Also, Navon et al. [13] have proposed an algorithm based on color image segmentation using a local threshold values. The aim of this technique is to partition an image into homogeneous regions by using a local threshold values. The threshold values are determined with the usage of merging process.

In the same way, S. ben chaabane et al [12] have proposed a segmentation approach based on homogeneity histogram and data fusion techniques. This technique is employed to merge different data sources in order to increase the quality of the information and to obtain an optimal segmented image. Also, Navon et al. [13] have proposed an algorithm based on color image segmentation using a local threshold values. The aim of this technique is to partition an image into homogeneous regions by using a local threshold values. The threshold values are determined with the usage of merging process. Histogram thresholding is one of the widely used techniques for gray level image segmentation [14] [15]. As for color images, the situation is different due to the multi-features. Since the color information is represented by the three component images R, G and B or some linear/nonlinear transformation of RGB, representing the histogram of a color image in the three dimensional (3-D) array and selecting threshold in the histogram is not a trivial job [16]. To solve this problem, several methods have been developed for storing and processing the information of the image in the 3-D color space. In this context, Gautier et al. [17] vise to furnish a help to the doctor for the follow-up of the maladies of the spinal column. The goal of this technique is to reconstruct each vertebral lumbar rachis from a set of cross-sections. The procedure is based on the operation of the belief theory to fusion information

With the same objective, Zimmermann and Zysno [18] have shown through empirical studies that the efficient Model for Membership Functions is defined as function of the Distance of a point from a prototypical member (MMFD). However, one of the dominant factors that impact the determination of convenient groups of points is the "distance measure" chosen for the problem at hand. Otsu's method [19] choose an optimum threshold by maximizing the between class variance in a gray image. However, the results proven are unsatisfactory. Huang and Wang [20] presented a version of Otsu's method in order to improve performance by reducing the computation cost for multilevel threshold.

In addition, Ohlander et al. [21] have demonstrated that the nine features (R, G, B, Y, I, Q, H, S and V) provided by the {RGB, YIQ and HSV} color spaces are redundant and complementary. In this context, image segmentation using data fusion techniques appears to be an interesting method. This paper is devoted to fuse nine redundant features provided by three different color spaces, applied to color image segmentation, where we aim at providing a help to the doctor for the follow-up of the diseases of the breast cancer. So, this work may be seen to be straightforwardly complementary to that in the paper proposed by Ohlander et al. [21]. In their paper, the authors suggested that the user has to search the significant peak in the histograms of the nine redundant features and then a threshold is determined to segment the input image. Although, selecting threshold in the histogram is not a trivial job. Hence, this paper is devoted to fuse one by one the pixels coming from different features provided by three color spaces. The idea is based on fuzzy clustering algorithm and data fusion techniques. The different informations are fused together by the DS evidence theory using as input features, the mass functions, previously estimated and associated to each pixel. The idea here is to assign a mass function to each information trough using the concept of fuzzy logic. To do this, a Fuzzy c-means (FCM) algorithm is used to

represent the input information as fuzzy sets. Each information is then characterized by its membership values in classes. The mass function assigned to a pixel for the classes are derived from the membership functions. Once the mass functions are determined for each image to be fused, the DS combination rule and decision are applied to obtain the final segmentation result. Section 2 introduces the proposed method for color image segmentation. The experimental results are discussed in Section 3, and the conclusion is given in Section 4.

2. The proposed method

In this section, a new method is introduced to segment the color cells images to decrease the adverse effects the uncertainty in segmentation. The FCM algorithm is applied to the images to be combined corresponding to the gray level to obtain the mass functions. The estimation of the mass functions of a single hypothesis is obtained with the membership of each gray level in each cluster. Multiple hypotheses are developed when the gray level can be assigned to several single hypotheses credibly. Then DS theory is used to fuse the pixels coming from the different images to be combined.

The objective is to rebuild each cell from a series of N redundant component images provided by the input image expressed in Ns color spaces. Hence, the idea of using the Dempster-Shafer (DS) evidence theory is to fuse one by one the feature vectors of each pixel coming from the nine redundant component images provided by the {RGB, YIQ and HSV} color spaces.

2.1. Fuzzy clustering

The standard Fuzzy C-means (FCM) algorithm is one of the widely used techniques for monochrome image segmentation. A comprehensive survey of fuzzy clustering methods is provided in [13] [14]. In this paper, we employ the concept of Fuzzy C-means algorithm to determine the mass function in the Dempster Shafer evidence theory as membership degrees.

Assume g_{xy} is the intensity of a pixel p_{xy} at the location (x, y) in an $(M \times N)$ image, $X = [x_1, x_2, ..., x_d]$ is the same data or information given in a Table must not be repeated in a Figure and vice versa. It is not acceptable to repeat extensively the numbers from Tables in the text or to give lengthy explanations of Tables or Figures.

vector containing all the gray level of the image, where $\{x_1 = g_{11}, x_2 = g_{12}, ..., x_d = g_{MN}\}$, n_c designate the number of clusters in which X will be classified and $V = [v_1, v_2, ..., v_{n_c}]$ is the vector of the cluster centers. A fuzzy n_c -partition of X is represented by a matrix $U = [u_{ik}]$, where $u_{ik} = u_i(x_k)$ expresses the membership degree of the element x_k in cluster i, and verifies the following constraints:

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$$\begin{cases} \sum_{i=1}^{n_c} u_{ik} = 1; & 1 \le i \le n_c, 1 \le k \le d \\ & u_{ik} \in [0, 1]; 1 \le i \le n_c \\ & \sum_{k=1}^d u_{ik} > 0; & 1 \le i \le n_c \end{cases}$$

In FCM algorithm, a good partition U of X is obtained by minimizing the objective

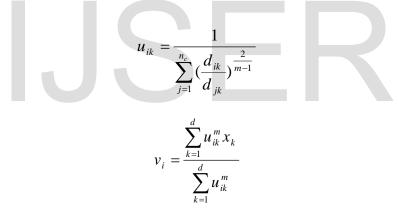
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$$J_m(u,v) = \sum_{k=1}^d \sum_{i=1}^{n_c} (u_{ik})^m ||x_k - v_i||^2$$

Where *m* is the fuzzy factor (m>1), $d_{ik} = ||x_k - v_i||$ is the distance between the

sample x_k and clustering center v_i .

In fact, (U, V) may minimize \boldsymbol{J}_m only if:



The proposed estimation mass function method using the standard FCM algorithm

is outline in the following steps:

Input an $(N \times M)$ image with gray levels zero to 255.

Step 1: Initialization (iteration 0)

Randomly initialize the centers of the classes vectors V(0) of size $(c \times 1)$ containing

the centers of the classes.

From the iteration t=1 to the end of the algorithm:

Step 2: Calculate the membership matrix U(t) of element u_{ik} using:

$$u_{ik} = \frac{1}{\sum_{i=1}^{n_c} (\frac{d_{ik}}{d_{jk}})^{\frac{2}{m-1}}}$$

In the modified method, the F_k and v_i are vectors of size (1×4) .

Step 4: Calculate the vector V(t) composed of 4 columns v_i using:

$$v_i = \frac{\sum_{k=1}^d u_{ik}^m x_k}{\sum_{k=1}^d u_{ik}^m}$$

Step 5: Convergence test:

If $\|V^{(t)} - V^{(t-1)}\| > \varepsilon$, then increment the iteration t, and return to the step 2, otherwise, stop the algorithm. ε is a chosen positive threshold.



2.2. Use of DS Evidence Theory for Image Segmentation

The proposed method consists to partition the color image into homogeneous

regions. The idea of using the DS evidence theory [22] [23] is to fuse one by

one the characteristic vectors of each pixel coming from the nine component

images {R, G, B, Y, I, Q, H, S and V} provided by the three redundant

{*RGB*, *YIQ* and *HSV*} color spaces.

To achieve that, the membership degrees of each pixel are estimated by using the

FCM algorithm. Then, a method is used to determine the simple and composite

classes in DS evidence theory from the obtained membership degree. Once the

mass functions are determined for each image to be fused, the DS combination

rule and decision are employed to merge the input images, in order to increase the

quality of the information and to obtain an optimal segmented image.

In the case of using the evidence theory for image segmentation, the determination of mass function is a crucial step of fusion process, and the performance of the segmentation scheme is, however, largely conditioned by the appropriate determination of the mass functions. In the present study, the method of generating the mass functions of the simple and double classes is performed in

fuzzy logic domain.

2.3.1 Mass Function of Simple Hypotheses

In our application, the number n_c of classes C_i will be taken as the number of the

simple hypotheses. These classes form the frame of discernment which is

symbolized by:

$$\{H_1, H_2, H_3, \dots, H_{n_c}\} = \{C_i\}; \ 1 \le i \le n_c$$

Masses of simple hypotheses H_i are directly obtained from the membership degree

 $u_{xy}(C_i)$ of the gray level g_{xy} at the location (x, y) in the q^{eme} image to be combined:

$$m_{xy}^q(\mathcal{C}_i) = u_{xy}^q(\mathcal{C}_i); 1 \le i \le n_c$$

This equation indicates that for a given gray level \boldsymbol{g}_{xy} of a pixel $\boldsymbol{p}_{xy}~$ at the location

(x,y) in the $q^{\diamond me}$ image to be combined, its share of belief placed strictly on \mathcal{C}_i is

directly given by its membership degree to the same cluster.

2.3.3 Mass Function of double Hypotheses

The mass function assigned to double hypotheses depends on the mass functions

of each hypothesis. Once the double hypotheses (composed of two simple

hypotheses) are formed, their joint mass is calculated according to the following formula:

$$m_{xy}^q (\boldsymbol{C}_i \cup \boldsymbol{C}_j) = (1 - u_{xy}^q (\boldsymbol{C}_i)) \cdot (1 - u_{xy}^q (\boldsymbol{C}_j));$$

In the case where the double hypotheses C_i are composed of more than two simple

hypotheses, their joint mass is determined as follows:

$$m_{xy}^{q}(C_{j} = C_{1} \cup C_{2} \cup ... \cup C_{M}) = \prod_{i=1}^{M} (1 - u_{xy}^{q}(C_{i})); 1 \le i \le M$$

2.3.3 The output fusion

Once the mass functions of the nine components images are estimated, their combination is performed using the orthogonal sum that can be represented as

follows:

1

with \oplus is the sum of DS orthogonal rule.

Specifically, the combination (called the joint $m^{12}\mbox{)}$ is calculated from the

aggregation of two mass functions m^1 and m^2 associated to the $\mathbf{1}^{th}$ and the $\mathbf{2}^{th}$

features, i.e., the Red and the Green features and given as follows:

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$$\forall C_i \subseteq \Omega, \qquad m^{12}(C_i) = \frac{1}{1-k} \sum_{A_1 \cap A_2 = C_i} m^1(A_1) . m^2(A_2)$$

where A_1 and A_2 are subsets of 2^Ω, and

K evaluates the conflict between the sources $S_1 \text{and}\ S_2.$

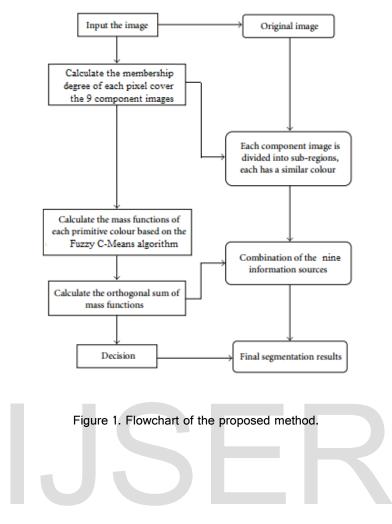
After calculating the orthogonal sum of the mass functions for the nine features, a

decision module is used for labeling each pixel respecting the combined mass

functions. The decisional procedure for classification purpose consists in choosing

one of the most likely hypotheses $C_i. \label{eq:constraint}$ The proposed method can be described by a

flowchart given in Figure 1.



3. Results

In order to illustrate the methods presented in the previous section, a large variety

of medical and synthetic color images are employed in our experiments. The used

images data base is shown in Figure 2.

In fact, to evaluate the efficiency and accuracy of the proposed segmentation

method, we applied the proposed method on color cells images. Also, a synthetic

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image dataset is developed and used for numerical evaluation purpose. The

segmentation results are compared versus existing methods, as described earlier.

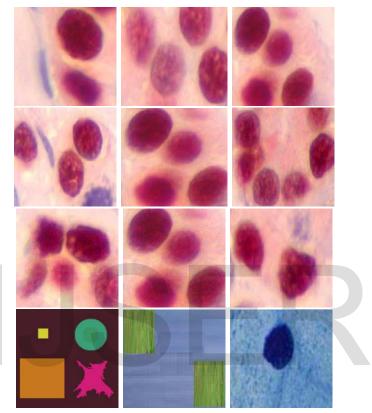


Figure 2: Data set used in the experiment. Twelve were selected for a comparison study.

The patterns are numbered from 1 through 12, starting at the upper left-hand corner. To illustrate the segmentation results obtained by the method based on data fusion techniques and fuzzy classification algorithm, called (DSFCM), we applied the modified fuzzy c-means algorithm to the input image of the figure (FIG. 3(a)) where the number of classes is limited to two and the fuzzy coefficient m is set to 2.

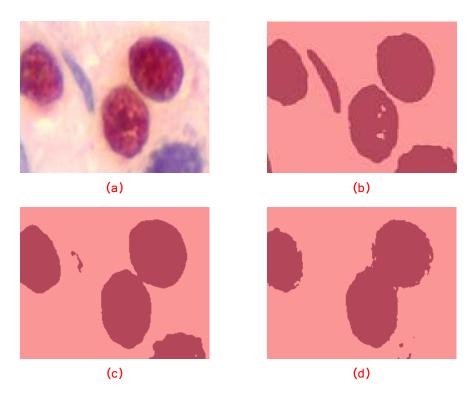


Figure 3: Segmentation results on a color image. (a) Original image (256×256×3) with gray level spread on the range [0, 255]. (b) Red resulting image by Fuzzy c-means algorithm. (c) Green resulting image by Fuzzy c-means algorithm. (d) Blue resulting image by byFuzzy c-means algorithm.

By applying the Fuzzy c-means algorithm independently to the component images of the input image expressed in the space color {RGB or YIQ or HSV}, does not give a better results and does not take sufficient account of the initial correlation. This shows that the use of a single information source leads to bad results.

The segmentation results obtained by applying the FCM algorithm to the red, green and blue color features are shown in Figs. 3(b), (c), and (d), respectively. In these figures, a label to each pixel corresponding to the class to which it belongs is affected. However, for easy viewing, the label of each class is selected

as the average color of the pixels that compose this class. It is noted that the two classes are not well built. In this context, image segmentation using data fusion techniques appears to be an interesting method. To do this, we propose to combine the results obtained by the Fuzzy C-means (FCM) algorithm applied independently to the nine component images of the original image represented in the three color spaces (RGB, HSV and YIQ).

Figure 3 shows a comparison between our method and other methods such as HHDS [13] and the method proposed by R. Harrabi et al. [23].

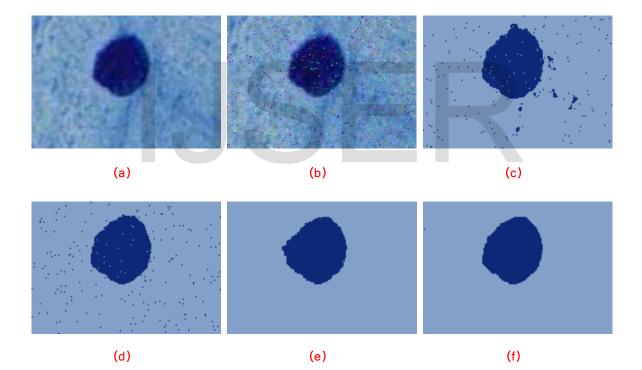


Figure 4: Comparison of the proposed segmentation method with other existing methods on a medical image (2 classes, 1 cell). (a) Original image with RGB representation (256 × 256 × 3), (b) color cell image disturbed with a "salt and pepper" noise, (c) segmentation based on HHDS method (d) segmentation based on MTDS method, (e) segmentation based on FCM algorithm and DS, and (f) reference segmented image.

However, the image shown in Figure 4(b) represents the original image I where a "salt and pepper" noise of D density was added. This affects approximately $D \times (N \times M)$ pixels. The value of D is 0.02. The figures 4(c), 4(d) and 4(e) show the segmentation results obtained by the methods (HHDS), (MTDS) and the proposed method (FCMDS), respectively. Fig 4(f) shows the ideal segmentation result (reference image).

In fact, one can find that the different objects presented in the original image are much better segmented in figure (FIG. 4(f)) than those in the figures (FIG. 4(c), and (d)). Consequently, the experimental results are improved by the proposed approach. So, the FCM algorithm can be used to produce mass functions that have typical interpretations, also, the resulting partition data can be interpreted as compatibility points with the different types of classes covering image.

The experimentation is carried out on medical images of cancer disease type in Fig. 5(a) and these images are used as original images. The segmentation results are obtained using the Gaussian distribution (GD), HCM and FCM clustering algorithms for the determination of the mass functions in the DS theory. They correspond, respectively, to Figs. 5(b), (c) and (d).

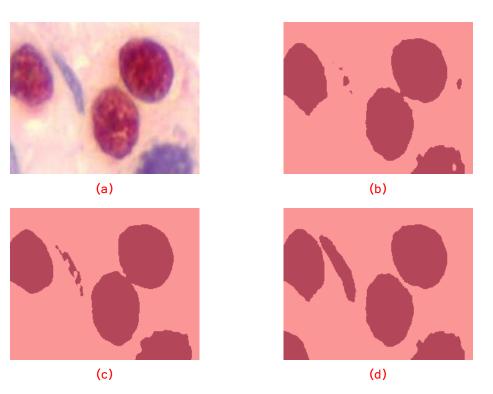


Figure 5: Comparison of the proposed segmentation method with other existing methods on a complex medical image (2 classes, various cells). (a) Original image ($256 \times 256 \times 3$): color medical image with RGB description, (b) segmentation based on HCM and DS, (c) segmentation based on GD and DS, and (d) segmentation based on FCM and DS.

Table 1. Segmentation sensitivity From HCMDS, HHDS, GDDS and FCMDS for the data set	t shown
in Fig. 2.	

	HCMDS	HHDS	GDDS	FCMDS (Proposed Method)	
	Segmentation sensitivity (%)				
Image 1	0.8245	0.8945	0.8647	0.9441	
Image 2	0.7845	0.8754	0.8712	0.9834	
Image 3	0.7513	0.8594	0.8996	0.9216	
Image 4	0.8112	0.8854	0.8455	0.8995	

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Image 5	0.7451	0.7964	0.8972	0.9462
Image 6	0.7845	0.8792	0.8324	0.8774
Image 7	0.6798	0.7811	0.7798	0.9726
Image 8	0.7215	0.7397	0.7894	0.9511
Image 9	0.7849	0.7987	0.8772	0.9349
Image 10	0.8561	0.8991	0.9247	0.9848
Image 11	0.8765	0.9248	0.9456	0.9821
Image 12	0.8936	0.9174	0.9228	0.9893

However, in the Gaussian model and standard fuzzy approach HCM, the

membership probability and the membership degree of each pixel, which leads to the presence of many incorrectly classified pixels. Hence, the cells are exactly and homogeneously segmented in Fig. 5(d), which is not the case in Fig. 5(b) and

(c).

Hence, the experimental results presented in Figure 5(d) are quite consistent with

the visualized color distributions in the objects, which make it possible to do an

accurate measurement of cell volumes.

In short, the proposed algorithm outperforms all these well-known segmentation

algorithms in terms of segmentation sensitivity (Sen(%)).

To evaluate the performance of the proposed segmentation algorithm, its accuracy

was recorded. Regarding the accuracy, Tables 1 lists the segmentation sensitivity

of the different methods for the data set used in the experiment. The segmentation

sensitivity [24] [25] is computed using:

$$Sens = \frac{N_{pcc}}{N \times M} \times 100,$$

whereSens, Npcc, N×M are respectively the segmentation sensitivity (%), number

of correctly classified pixels and dimension of the image.

The performance of the proposed method is quite acceptable. In fact, from table 1, one can observe in Figures 5(b), 5(c), and 5(d) that 18.88%, 15.45% and

10.05% of pixels were incorrectly segmented for the HCMDS, GDDS and FCMDS

methods, respectively.

This experiment shows the validity of our fusion procedure and also the significant

improved performance in segmentation.

The three images, shown in Fig.5 (b), (c) and (d), were used in order to visually

assess the quality of segmentation results.

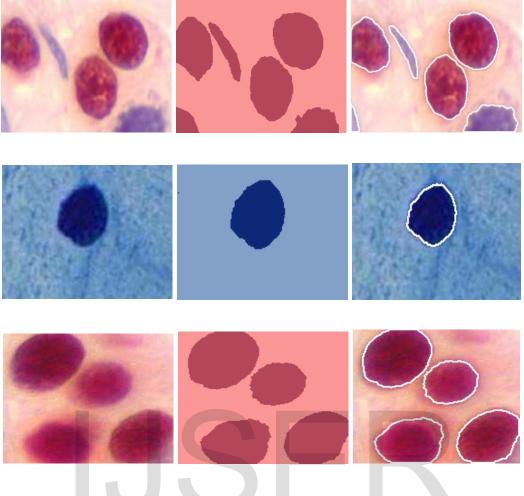


Figure 6. Color edges detection.

In fact, from an initial segmentation obtained by using the fuzzy c-means, one

seeks a segmentation which means to detect the cells in medical images of cancer

disease (see Fig. 5(d)), as also the number of the cells. Consequently, the

proposed method can be useful for color image segmentation.

Figure 6 illustrates the final results for the three images selected from the used images data base (Fig.5), where the edges in white color are superimposed on the original images.

4. Conclusion

In this paper, we have proposed a new color image segmentation method for based on Fuzzy C-means algorithm and Dempster-Shafer evidence theory. This method consists of two steps. In the first step, the automatic estimation of mass functions in the DS evidence theory is determined from the Fuzzy C-means algorithm. In the second step, the DS combination rule and decision are applied to fuse the nine components images of the input image expressed in three-color spaces.

The proposed segmentation approach is conceptually different and explores a new strategy. In fact, instead of considering only one image for each application, many component images of the same image fused together may be very helpful to the segmentation process. The idea is to fuse one by one the pixels coming from different information sources, in order to get a final reliable and accurate

segmentation result.

The obtained results demonstrated the significant improved performance in

segmentation. The proposed method can be useful for color image segmentation.

References

[1] I. Bloch, "Information combination operators for data fusion: A comparative review with classification," IEEE Trans. SMC, vol. 26, no.1, pp.52-67, 1995.

[2] Y. Yang, Ch. Zheng and P. Lin, "Fuzzy C-means clustering algorithm with a novel penalty term for image segmentation", Opto-Electronics Rev., vol. 13, no. 4, pp.309-315, 2005.

[3] V. Grau, A. U. J. Mewes, M. Alcaniz, R. Kikinis, and S. K. Warfield, "Improved

watershed transform for medical image segmentation using prior information", IEEE

Transactions on Medical Imaging, vol. 23, no. 4, pp. 447-458, 2004.

[4] R. O. Duda, P. E. Hart, and D. G. Sork, "Pattern Classification", Wiley-Interscience,

New York, NY, USA, 2000.

[5] S. Ben Chaabane, M. Sayadi, F. Fnaiech, E. Brassart, "Dempster-Shafer Evidence Theory for Image Segmentation: Application in Cells Images," International Journal of Signal Processing, vol. 5, no. 1, pp. 126-132, 2009.

[6] R. Harrabi and E. Ben Braiek, "A comparative study of color image segmentation

techniques using different color representation, pp. 1-6, JTEA, Tunisia, 2010.

[7] D. Y. Huang and C. H. Wang, "Optimal multi-level thresholding using a two-stage

Otsu optimization approach", Pattern Recognition Letters, vol. 30, pp. 275-284, 2009.

[8] M. Mignotte, "Segmentation by Fusion of Histogram-Based K-Means Clusters in

Different Color Spaces", IEEE Trans. on Imag. Proc., vol. 17, no. 5, pp. 780-787, 2008.

[9] H. D. Cheng, X. H. Jiang and J. Wang, "Color image segmentation based on homogram thresholding and region merging", Pattern Recognition, vol. 25, pp. 373-393, 2002.

[10] I. Bloch, H. Maitre, "Fusion of image information under imprecision, in: B. Bouchon-Meunier (Ed.), Aggregation and fusion of imperfect information," Series studies in fuzziness, Physical Verlag, Springer, pp. 189–213, 1997. [11] I. Bloch, "Information combination operators for data fusion: A comparative review

with classification," IEEE Trans. SMC, vol. 26, no.1, pp.52-67, 1995.

[12] D. Shao-Long; W. Jian-Ming; X. Tao; L. Hai-Tao, "Constraint-based Fuzzy

Optimization Data Fusion for Sensor Network Localization", Second International

Conference on Semantics Knowledge and Grid, SKG '06, pp. 59-59, 2006.

[13] S. B. Chaabane, M. Sayadi, F. Fnaiech and E. Brassart, "Colour Image

Segmentation using Homogeneity approach and Data Fusion Techniques", Eurasip journal

on advances in signal processing, vol. 2010, ID. 367297, pp. 1-11, 2010.

[14] R. Harrabi and E. Ben Braiek, "Color image Segmentation using automatic thresholding techniques," pp. 1-6, SSD'2011, Tunisia, 2011.

[15] S. Ben Chaabane, M. Sayadi, F. Fnaiech and E. Brassart, "Color Image Segmentation using Automatic Thresholding and the Fuzzy C-Means Techniques," IEEE Mediterranean Electrotechnical Conference, MELECON'2008, pp. 857-861, Ajaccio– France, 2008.

[16] S. B. Chaabane, M. Sayadi, F. Fnaiech and E. Brassart, "Estimation of the Mass Function in the Dempster-Shafer's Evidence Theory using Automatic Thresholding for Color Image Segmentation", International Conference on Signals, Circuits and Systems,

SCS'08, pp. 1-5, Tunisia, 2008.

[17] L. Gautier, A. Taleb-Ahmed, M. Rombaut, J. G. Postaire and H. Leclet, "Decision

support of image segmentation by the Dempster-Shafer theory: application to a sequence

of IRM images", Edit. Sc. et med. Elsevier SAS, vol. 22, pp.378-392, 2001.

[18] H. J. Zimmerman and P. Zysno, "Quantifying vagueness in decision models,"

European J. Operational Res., vol. 22, pp. 148-158, 1985.

[19] N.Ots, A threshold selection method from gray_level histograms, IEEE Trans. on Sys., Man, Cybern., vol.9, pp.62-69,1979.

[20] D. Y. Huang and C. H. Wang, "Optimal multi-level thresholding using a two-stage

Otsu optimization approach", Pattern Recognition Letters, vol. 30, pp. 275-284, 2009.

[21] A. P. Dempster, "Upper and lower probabilities induced by multivalued mapping",

Annals of Mathematical Statistics, vol. 38, pp. 325-339, 1967.

[22] S. B. Chaabane, M. Sayadi, F. Fnaiech, E. Brassart and F. Betin, "A New Method

for the Mass Functions Estimation in the Dempster-Shafer's Evidence theory: Application

to color Image Segmentation", Circuits systems and signal processing, vol.30, pp. 55-71,

2011.

[23] R. Harrabi and E. Ben Braiek, "Color image segmentation using multi-level

thresholding approach and data fusion techniques: application in the breast cancer cells

images", EURASIP Journal on Image and Video Processing, 2011.

[24] V. Grau, A. U. J. Mewes, M. Alcaniz, R. Kikinis, and S. K. ~ Warfield, "Improved

watershed transform for medical image segmentation using prior information," IEEE

Transactions on Medical Imaging, vol. 23, no. 4, pp. 447-458, 2004.

JS

[25] R. O. Duda, P. E. Hart, and D. G. Sork, Pattern Classification, Wiley-Interscience,

New York, NY, USA, 2000.